OPTIMIZATION OF N-QUEENS PROBLEM USING HYBRID MEMETIC ALGORITHMS

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ABSTRACT

The problems like N-Queens problem are non-polynomial time problems. In this research study, we use the MA to optimize NP hard problem i.e N-Queens problem and make complexity analysis on some parameters with respect to number of iterations. The MA is a hybrid algorithm, being a combination of the Genetic Algorithm (GA) and a local search algorithm. The performance of the MA is found to be superior to that of GA. The MA solves the N-Queens in two stages, in the first stage, the randomly generated solutions are evolved till they become feasible (i.e., the hard constraints are satisfied) and in the second stage, these solutions are further evolved so as to minimize the violations of the soft constraints. In the final stage, the MA produces optimal solutions in which the hard as well as the soft constraints are completely satisfied.

Keyword: - *Queens, N-Queens, 8 Queens, Genetic Algorithm, Chromosome, Mutation, Selection, Crossover, Recombination, GA, MA.*

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1. Introduction

Problems with non-deterministic solutions that run in polynomial time are called NP-class problems. Because of their high complexity (e.g. O(2n) or O(n!)) they cannot be solved in a realistic timeframe using deterministic techniques. To solve these problems in a reasonable amount of time, heuristic methods must be used.
N-Queens problem which is to place the ‘n’ numbers of Queens on a chess board so that neighbor Queens cannot contradict each other vertically, horizontally and diagonally. Some of the recent AI techniques include the use of simulated annealing, hill-climbing, genetic algorithm, co-operative genetic algorithm, artificial immune system and different versions of evolutionary algorithms. The conventional GA does not yield satisfactory solutions. Therefore, we believe that a hybrid methodology involving an Evolutionary Algorithm that finds several feasible solutions and a Local Search exploiting the inherent knowledge of the problem to optimize the intermediate feasible solutions is an appropriate tool to tackle this highly complex problem. The hybridization of evolutionary algorithms (EAs) with other techniques can greatly improve the efficiency of search. EAs hybridized with local search techniques are named as Memetic Algorithms .A common approach is to apply the local search to the GA population after crossover and mutation, with the aim of exploiting the best search regions. An important aspect concerning MAs is the trade-off between the exploration abilities of the EA and the exploitation abilities of the local search technique.

In this study, we use a Memetic Algorithm (MA) to solve the complex n-Queens problem. The MA algorithm is a hybrid of the Genetic Algorithm (GA) and Local Search (LS). The GA follows a simple coding scheme and after the recombination operations, LS is applied using problem-specific knowledge. A number of random shift schedules are generated. Penalties are imposed for the violation of the hard as well as the soft constraints of the shift schedules. The MA solves the problem in two phases. In the first phase, it tries to resolve all the violations of the hard constraints. This leads to feasible solutions. In the second phase, MA works with the feasible solution and further evolves them eliminating, or at least minimizing the soft constraints. The result is optimal solutions satisfying the n-Queens problem.
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2. N-Queens Problem (NQP)

The classic combinatorial problem is to place N-Queens on a chessboard so that no two attack each other. This problem can be generalized as placing ‘n’ non attacking queens on an N × N chessboard. Since each queen must be on a different row and column, we can assume that queen ‘i’ is placed in i^{th} column. All solutions to the NQP can therefore be represented as n-tuples (q1, q2, …, q^n) that are permutations of an n-tuple (1, 2, 3, …, n). Position of a number in the tuple represents queen's column position, while its value represents queen's row position (counting from the bottom) using this representation, the solution space where two of the constraints (row and column conflicts) are already satisfied should be searched in order to eliminate the diagonal conflicts. Complexity of this problem is O(n!). [1]

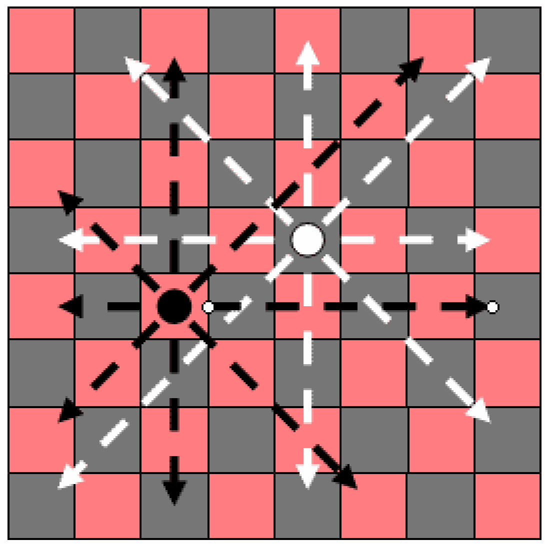

Fig -1.Chess board of size 8*8 with 8 queens. [2][4]

3. Optimization

Optimization is the process of identifying the best solution among a set of alternatives. Single objective optimization employs a single criterion for identifying the best solution among a set of alternatives. [1]

1. Read the problem.
2. Reread the problem.
3. Draw a picture or graph if appropriate.
4. Identify the given information – What are the variables? – What are the constants? – Are there any constraints? – Label the graph or picture.
5. What quantity needs to be maximized or minimized?
6. Find an appropriate equation for what needs to be maximized or minimized, and reduce it to one variable.
7. Find the derivative and critical points for your equation.
8. Test your critical points and end points (where appropriate).
9. Reread the question and make sure you have answered what was asked.

4. N-Queens optimization using Memetic Algorithm

The Memetic Algorithm (MA) we have used to solve the above QMC n-Queens consists of the Genetic Algorithm combined with a local search. The MA flowchart is shown in Fig. 1. It describes in detail each of the steps of the MA. Steps of Memetic Algorithm are given below:

1. **Random Generation**
2. **Fitness &Selection**
3. **Crossover**
4. **Mutations**
5. **Local Search**

5. Applications of N-Queens

These are given below:

1. VLSI Testing.
2. Traffic control.
3. Deadlock Prevention.
4. Image Processing.
5. Motion Estimation.
6. Register Allocation. [6]

6. Results

The below graphs show the results of applying the MA for the optimization of N-Queens problem. In this research paper the tables show that MA gives best results in comparison of GA in terms of space complexity as the number of iterations and number of queen's increases. In terms of optimal solutions MA gives best solutions than GA. Then convergence rate checked between these techniques MA has best convergence rate than GA on different number of iterations and number of queens. Then time complexity calculated between three approaches MA has less time complexity than GA for different number of iterations and number of queens.

Table -1. Optimal solutions based on the number of Queens (n) and number of iterations=5.

No of Queens	GA	SALSMA	HCLSMA
8	5	5	5
16	2	3	5
24	0	1	5
32	0	1	5
40	0	0	5

Table -2. Optimal solutions based on the number of Queens (n) and number of iterations=8.

No of Queens	GA	SALSMA	HCLSMA
8	8	8	8
16	1	5	8
24	0	2	8
32	0	1	8
40	0	0	8

Table -3. Optimal solutions based on the number of Queens (n) and number of iterations=10.

No of Queens	GA	SALSMA	HCLSMA
8	10	10	10
16	2	5	10
24	0	3	10
32	0	1	10
40	0	0	10

Table -4. Convergence rate based on the number of Queens (n) and number of iterations=5.

No of Queens	GA	SALSMA	HCLSMA
8	100	100	100
16	40	60	100
24	0	20	100
32	0	20	100
40	0	0	100

Table -5. Convergence rate based on the number of Queens (n) and number of iterations=8.

No of Queens	GA	HCLSMA	HCLSMA2
8	100	100	100
16	12.5	62.5	100
24	0	25	100
32	0	12.5	100
40	0	0	100

Table -6. Convergence rate based on the number of Queens (n) and number of iterations=10.

No of Queens	GA	SALSMA	HCLSMA
8	100	100	100
16	20	50	100
24	0	30	100
32	0	10	100
40	0	0	100

Table -7. Time complexity based on the number of Queens (n) and number of iterations=5.

S.No.	No of Queens (n)	HCLSMA (ms)	SALSMA (ms)	GA (ms)
1	8	3420	3481	3606
2	16	46165	46201	46236
3	24	192104	192131	192157
4	32	187950	187987	188023
5	40	1577690	1577719	1577752

Table -8. Time complexity based on the number of Queens (n) and number of iterations=8.

S.No.	No of Queens (n)	HCLSMA (ms)	SALSMA (ms)	GA (ms)
1	8	3565	3595	3627
2	16	101821	101865	101903
3	24	160832	160867	160903
4	32	458919	458935	458951
5	40	1486878	1486913	1486949

Table -9. Time complexity based on the number of Queens (n) and number of iterations=10.

S.No.	No of Queens (n)	HCLSMA (ms)	SALSMA (ms)	GA (ms)
1	8	3607	3633	3660
2	16	121636	121674	121709
3	24	296828	296863	296900
4	32	756203	756238	756274
5	40	2550705	2550722	2550741

7. Conclusion and Future-Work

Some studies show that the straight forward implementation of the Genetic Algorithm is incapable of obtaining a satisfactory solution. Therefore, we believe that a hybrid methodology involving an Evolutionary Algorithm that finds several feasible solutions and a Local Search exploiting the inherent knowledge of the problem to optimize the intermediate feasible solutions is an appropriate tool to tackle this highly complex problem. With this intuition, we have a Memetic Algorithm (GA + local search) to solve the NQP. The hybrid MA solves the NQP in two phases. In the first phase it tries to search for the Queens's shift patterns that do not violate the hard constraints. MA gives better results than GA for optimal solutions, time and convergence rate. Future work includes the parameters like conflict minimization and revolution rate for the comparison of MA and GA.

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