

REAL LIFE APPLICATION OF TRANSPORTATION PROBLEM IN MALAYSIAN PETROCHEMICAL COMPANY

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INTRODUCTION

The Petrochemical Industry is one of the leading industries in Malaysia. From being an importer of petrochemicals, Malaysia today is an exporter of major petrochemical products. A wide range of petrochemicals such as olefins, polyofins aromatics, ethylene oxides, poly vinyl chloride are produced in these industries. The Malaysian Petrochemical Company '**Petronas**' was established in 1974 and is wholly owned by the Government of Malaysia, the corporation is vested with the entire oil and gas resources in Malaysia and is entrusted with the responsibility of developing and adding value to these resources. Fortune ranks Petronas as the 158th largest company in the world in 2019.

In 2006, Economic times published an article stating that Mitco Labuan the trading arm of the \$44.3 billion Malaysian Petrochemical giant Petronas was setting up a wholly owned subsidiary to engage in trading and related in the country.

The trading company '**Mitco Labuan**', wholly owned subsidiary of the Malaysian Petrochemical Company is involved in buying and selling poly vinyl chloride polymer. The polymer is produced by four petrochemical plants in Malaysia and is exported to four destinations namely China, the Middle East, Europe and South East Asia.

APPLICATION OF TRANSPORTATION PROBLEM

The production capacity of each polymer producing Petrochemical Plant are

Polymer producing Petrochemical Plant	Production Capacity (thousands tons per annum)
P1	110
P2	75
P3	95
P4	125

The demand of the customers is

Destination	Shipment Quantity (thousands tons per annum)
China (D1)	200
Middle East (D2)	90

South East Asia (D3)	40
Europe (D4)	45

Each Plant has a fixed capacity per annum that shall be distributed to the customers. Similarly, each destination has a fixed demand per annum that must be fulfilled from the various plants.

The Shipping costs from the polymer producing petrochemical plants to the various destinations are

Unit Cost of Shipping (RM '000) (RM = Malaysian Ringgit)

Plant	China	Middle East	South East Asia	Europe
P1	200	300	100	600
P2	400	350	150	650
P3	300	250	150	600
P4	500	400	200	700

The unit cost of shipping varies as a result of differences in among others distance and also currencies exchange rates. Hence, allocating the production capacities to the various demand destinations in the optimal way to minimize total cost of shipping is crucial for the trading company.

Mathematical and spreadsheet formulation

The formulation of the transportation problem for this case study is aimed at determining the optimum allocation of production capacity to each demand destinations to minimize the cost of shipping. There are four polymer producing plants and four demand destination under consideration.

Units Costs	Destinations				Production Capacity
	D1	D2	D3	D4	
P1	200	300	100	600	110
P2	400	350	150	650	75
P3	300	250	150	600	95
P4	500	400	200	700	125
Demand	200	90	40	45	

(Unit Cost RM '000) (Demand and Production Capacity '000)

The demand is not equal to the production capacity therefore the solution is not balanced. To balance the solution, we assume a dummy column D5 with a demand of 30. Now Demand = Production Capacity thus the solution is balanced.

Unit Costs	Destinations					Production Capacity
	D1	D2	D3	D4	D5	
P1	200	300	100	600	0	110
P2	400	350	150	650	0	75
P3	300	250	150	600	0	95
P4	500	400	200	700	0	125
Demand	200	90	40	45	30	405

(Unit Cost RM '000) (Demand and Production Capacity '000)

Using Vogel's Approximation Method (VAM)

Unit Cost	Destinations					Production Capacity	T1	T2	T3	T4	T5	T6
	D1	D2	D3	D4	D5							
P1	200 (110)	300	100	600	0	110	100	100	100	-	-	-
P2	400 (35)	350	150 (40)	650	0	75	150	200	50	50	250	250
P3	300 (5)	250 (90)	150	600	0	95	150	100	50	50	300	-
P4	500 (50)	400	200	700 (45)	0 (30)	125	200	200	100	100	200	200
Demand	200	90	40	45	30	405						
T1	100	50	50	0	0							
T2	100	50	50	0	-							
T3	100	50	-	0	-							
T4	100	100	-	50	-							
T5	100	-	-	50	-							
T6	100	-	-	50	-							

(Unit Cost RM '000) (Demand and Production Capacity '000) (T is used to indicate penalties as P is used to indicate Petrochemical plants)

Rim Condition: $m+n-1$ = number of allocations

$m+n-1 \Rightarrow 4+5-1 = 8$; number of allocations = 8

Therefore, the solution is non degenerate.

Using Modified Distribution Method (MODI)

For Optimality, MODI – we'll find u_i and v_j .

Unit Cost	Destinations					Production Capacity	u_i
	D1	D2	D3	D4	D5		
P1	200(110)	300	100	600	0	110	0
P2	400(35)	350	150(40)	650	0	75	200
P3	300(5)	250(90)	150	600	0	95	100
P4	500(50)	400	200	700(45)	0(30)	125	300
Demand	200	90	40	45	30	405	
v_j	200	150	-50	400	-300		

(Unit Cost RM '000) (Demand and Production Capacity '000)

For occupied cells $\Rightarrow C_{ij} = u_i + v_j$

For unoccupied cells $\implies \Delta_{ij} = C_{ij} - (u_i + v_j)$

$P1D2 = 150 \quad P2D2 = 0 \quad P3D3 = 100 \quad P4D2 = -50$

$P1D3 = 150 \quad P2D4 = 50 \quad P3D4 = 100 \quad P4D3 = -50$

$P1D4 = 200 \quad P2D5 = 100 \quad P3D5 = 200$

$P1D5 = 300$

Since $\Delta_{ij} \leq 0$, the solution is not optimum as $P4D2$ and $P4D3$ are -50 .

After looping $P4D3$

Cell	Old Value	New Value
P4D3	0 +	40
P2D3	40 -	0
P2D1	35 +	75
P4D1	50 -	10

New table:

Unit Cost	Destinations					Production Capacity	u_i
	D1	D2	D3	D4	D5		
P1	200(110)	300	100	600	0	110	0
P2	400(75)	350	150	650	0	75	200
P3	300(5)	250(90)	150	600	0	95	100
P4	500(10)	400	200(40)	700(45)	0(30)	125	300
Demand	200	90	40	45	30	405	
v_j	200	150	-100	400	-300		

(Unit Cost RM '000) (Demand and Production Capacity '000)

For occupied cells $\implies C_{ij} = u_i + v_j$

For unoccupied cells $\implies \Delta_{ij} = C_{ij} - (u_i + v_j)$

$P1D2 = 150 \quad P2D2 = 0 \quad P3D3 = 150 \quad P4D2 = -50$

$P1D3 = 200 \quad P2D3 = 50 \quad P3D4 = 100$

$P1D4 = 200 \quad P2D4 = 50 \quad P3D5 = 200$

$P1D5 = 300 \quad P2D5 = 100$

Since $\Delta_{ij} \leq 0$, the solution is not optimum as $P4D2$ is -50 .

After looping P4D2

Cell	Old Value	New Value
P4D2	0 +	10
P2D3	10 -	0
P2D1	5 +	15
P4D1	90 -	80

New table:

Unit Cost	Destinations					Production Capacity	ui
	D1	D2	D3	D4	D5		
P1	200(110)	300	100	600	0	110	0
P2	400(75)	350	150	650	0	75	200
P3	300(15)	250(80)	150	600	0	95	100
P4	500	400(10)	200(40)	700(45)	0(30)	125	250
Demand	200	90	40	45	30	405	
vj	200	150	-50	450	-250		

(Unit Cost RM '000) (Demand and Production Capacity '000)

For occupied cells $\implies C_{ij} = u_i + v_j$

For unoccupied cells $\implies \Delta_{ij} = C_{ij} - (u_i + v_j)$

$P1D2 = 150$ $P2D2 = 0$ $P3D3 = 100$ $P4D1 = 50$

$P1D3 = 150$ $P2D3 = 0$ $P3D4 = 50$

$P1D4 = 150$ $P2D4 = 0$ $P3D5 = 150$

$P1D5 = 250$ $P2D5 = 50$

Since $\Delta_{ij} \geq 0$, the solution is optimum.

Therefore, the Optimum transportation cost (Unit Cost RM '000) (Demand and Production Capacity '000) =

$$200 \cdot 110 + 400 \cdot 75 + 300 \cdot 15 + 250 \cdot 80 + 400 \cdot 10 + 200 \cdot 40 + 700 \cdot 45 + 0 \cdot 30 = 120000$$

Therefore, the minimum transportation cost is $120000 \cdot 1000 \cdot 1000 = \text{RM } 120000$ million.

The solution isn't unique as $P2D2, P2D3, P2D4 = 0$. Thus, Alternate optimum soln. exists.

Alternate Optimum Solution:

After looping P2D4

Cell	Old Value	New Value
P2D4	0 +	45
P4D4	45 -	0
P4D2	10 +	55
P3D2	80 -	35
P3D1	15 +	60
P2D1	75 -	30

New Table:

Unit Cost	Destinations					Production Capacity	ui
	D1	D2	D3	D4	D5		
P1	200(110)	300	100	600	0	110	0
P2	400(30)	350	150	650(45)	0	75	200
P3	300(60)	250(35)	150	600	0	95	100
P4	500	400(55)	200(40)	700	0(30)	125	250
Demand	200	90	40	45	30	405	
vj	200	150	-50	450	-250		

(Unit Cost RM '000) (Demand and Production Capacity '000)

For occupied cells $\implies C_{ij} = u_i + v_j$

For unoccupied cells $\implies \Delta_{ij} = C_{ij} - (u_i + v_j)$

$P1D2 = 150 \quad P1D5 = 250 \quad P2D5 = 50 \quad P3D5 = 150$

$P1D3 = 150 \quad P2D2 = 0 \quad P3D3 = 100 \quad P4D1 = 50$

$P1D4 = 150 \quad P2D2 = 0 \quad P3D4 = 50 \quad P4D4 = 0 \quad \Delta_{ij} \geq 0$, the solution is optimum.

Therefore, Optimum Transportation Cost (Unit Cost RM '000) (Demand and Production Capacity '000) = RM 120000 million ($200 \times 110 + 400 \times 30 + 300 \times 60 + 250 \times 35 + 400 \times 55 + 200 \times 40 + 650 \times 45 + 0 \times 30 = 120000 \times 1000 \times 1000$)

Another Alternate optimum soln. exists as $P2D2, P2D3, P4D4 = 0$ (Another Alternate solution to be found to match the optimum solution provided in the research paper so one more looping is to be done from P2D2.)

After looping P2D2

Cell	Old Value	New Value
P2D2	0 +	30
P2D1	30 -	0
P3D1	60 +	90
P3D2	35 -	5

New table:

Unit Cost	Destinations					Production Capacity	ui
	D1	D2	D3	D4	D5		
P1	200(110)	300	100	600	0	110	0
P2	400	350(30)	150	650(45)	0	75	200
P3	300(90)	250(5)	150	600	0	95	100
P4	500	400(55)	200(40)	700	0(30)	125	250
Demand	200	90	40	45	30	405	
vj	200	150	-50	450	-250		

(Unit Cost RM '000) (Demand and Production Capacity '000)

For occupied cells $\implies C_{ij} = u_i + v_j$

For unoccupied cells $\implies \Delta_{ij} = C_{ij} - (u_i + v_j)$

$P1D2 = 150$ $P2D1 = 0$ $P3D3 = 100$ $P4D1 = 50$

$P1D3 = 150$ $P2D3 = 0$ $P3D4 = 50$ $P4D4 = 0$

$P1D4 = 150$ $P2D5 = 50$ $P3D5 = 150$

$P1D5 = 250$

Since $\Delta_{ij} \geq 0$, the solution is optimum.

Therefore, the Optimal transportation cost (Unit Cost RM '000) (Demand and Production Capacity '000) =

$200 \cdot 110 + 300 \cdot 90 + 350 \cdot 30 + 250 \cdot 5 + 400 \cdot 55 + 200 \cdot 40 + 650 \cdot 45 + 0 \cdot 30 = 120000$

Therefore, the minimum transportation cost is $120000 \cdot 1000 \cdot 1000 = \text{RM } 120000$ million.

Transportation Schedule:

Cell	Cost (RM'000)	Allocation ('000)	Total Cost ('000)
P1D1	200	110	22000
P3D1	300	90	27000
P2D2	350	30	10500
P3D2	250	5	1250
P4D2	400	55	22000
P4D3	200	40	8000
P2D4	650	45	29250
P4D5	0	30	0
OPTIMUM COST			RM 120000 million

CONCLUSION

Effective and efficient movement of products or services from point of supply to points of demand is crucial for any business. Transporting finished products to the market at the lowest possible costs leads to huge potential of cost savings and consequently maximize company’s profits. As such, the Company seeks to optimize their distribution plan for their products in relation to the cost of transportation with the help of a trading company.

The study highlighted the applications of VAM and MODI in form of linear programming and spreadsheet in a case study of a transportation problem of a Malaysian Petrochemical Company.

Optimum plan and solution to minimize the total cost of transportation were formulated and analysed.

After VAM, MODI was used to check the optimality of the allocations. But on examining it was inferred that Δ_{ij} values of Δ_{ij} were negative. So looping was performed not once but twice to remove the negativity of Δ_{ij} .

Since all the Δ_{ij} values were non negative, the solution was optimal. Although there were multiple values of Δ_{ij} to be zero therefore the solution wasn’t unique and hence alternate solutions were possible. Consequently, the alternate solutions resulted in identical output as in the research paper

The optimal transportation cost is RM 120000 million.

Therefore, we can conclude that linear programming is an alternative decision tool available to engineers and managers alike in ensuring their operations are conducted effectively and efficiently at the lowest cost possible and consequently helps company maximize its profits.

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